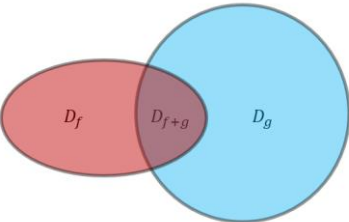


9.1 Exploring Combinations of Functions

<p>A Arithmetic Combinations</p> <p>Consider two functions $f(x)$ and $g(x)$. Then the sum $f + g$, difference $f - g$, product fg and the quotient f / g are defined as follows:</p> $(f + g)(x) = f(x) + g(x)$ $(f - g)(x) = f(x) - g(x)$ $(fg)(x) = f(x)g(x)$ $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}, \quad g(x) \neq 0$	<p>Ex 1. Given $f(x) = x^2 - 1$ and $g(x) = 2\sqrt{x-1}$, find:</p> <p>a) $(f + g)(1)$</p> <p>b) $(f - g)(2)$</p> <p>c) $(fg)(5)$</p> <p>d) $\left(\frac{f}{g}\right)(1)$</p> <p>e) $(f + g)(x)$</p> <p>f) $(f - g)(x)$</p> <p>g) $(fg)(x)$</p> <p>h) $\left(\frac{f}{g}\right)(x)$</p>
<p>B Domain</p> <p>The domain of $f + g$, $f - g$, and fg is $D_f \cap D_g$ (the intersection between the domain of f and the domain of g) (see diagram below).</p>  <p>The domain of $\frac{f}{g}$ is $\{x \in D_f \cap D_g \mid g(x) \neq 0\}$.</p>	<p>Ex 2. Given $f(x) = x^2 - 1$ and $g(x) = \sqrt{x-2}$, find the domain of the following arithmetic combinations:</p> <p>a) $(f + g)(x)$</p> <p>b) $(f - g)(x)$</p> <p>c) $(fg)(x)$</p> <p>d) $\left(\frac{f}{g}\right)(x)$</p> <p>e) $\left(\frac{g}{f}\right)(x)$</p>
<p>Ex 3. The function f has the x-intercepts -1, 1, and 3 and the y-intercept is 4. The function g has the x-intercepts -2 and -1 and the y-intercept is 1. Find the x-intercepts and the y-intercept of the following arithmetic combinations:</p>	<p>a) $(fg)(x)$</p> <p>b) $\left(\frac{f}{g}\right)(x)$</p> <p>c) $\left(\frac{g}{f}\right)(x)$</p>

Reading: Nelson Textbook, Pages 518-520

Homework: Nelson Textbook, Page 520#2,3